## CALIFORNIA STATE UNIVERSITY DEPARTMENT OF STATISTICS

## Statistics 4866/6871: Seminar - Introduction to Times Series Analysis Summer 2005

## Take-home Midterm

**Instructions:** This is a take-home exam. Your are expected to work on the exam alone. If you have questions about the exam you may ask the instructor.

- 1. (Stat 4866/6871) (Average Air Temperature Racife Brazil, 1953-1962.) The following problem is to describe and understand the variation in the temperature data.
  - (a) Plot the data  $\{x_t\}$  and describe its main features.
  - (b) Perform a Classical Decomposition of the data,  $X_t = S_t + T_t + I_t$ .
  - (c) Are there any unusual years in the data?
- 2. (Stat 4866/6871) (Yield on short-term British government securities.) Find a suitable time-series model and compute forecasts up to 12 months ahead.
  - (a) Plot the data and describe its main features. Is there a seasonal pattern?
  - (b) Suggest and apply an appropriate transformation that transforms the data to a stationary time series.
  - (c) Fit an ARIMA model to this set of data and justify your choice by examining the appropriate ACF, PACF, and residual plots.
  - (d) Give the estimated model and the value of the AIC.
  - (e) Calculate the formula for the one-step ahead forecast  $x_{n+1}^n$ .
  - (f) Forecast the time series 12 months ahead. Comment.
- 3. (Stat 4866/6871) (Monthly totals of international airline passengers, Jan. 1949 to Dec. 1960.) Fit an ARIMA model to the data and produce forecasts up to one year ahead.
  - (a) Plot the data and describe its main features.
  - (b) Suggest and apply a transformation that stabilizes the variance of the data.
  - (c) Suggest and apply a transformation that transforms the data to a stationary time series.
  - (d) Identify an appropriate ARIMA model for this set of data and specify any goodness-of-fit methods used in your selection process.
- 4. (Stat 6871) Problem 2.19, page 205.
- 5. (Stat 6871) Determine the best exponential smoothing forecasts for the three time series in the construction data.
- 6. (Stat 6871) Run the decomposition program for the electricity data and comment on the components of the time series.