# **Nearest Neighbors**

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### Introduction

We will begin discussing Classification using Nearest Neighbors.

According to the author, nearest neighbors classifiers are defined by their classifying of unlabeled observations/examples by assigning them the class of the most similar labeled observations/examples.

## k-NN algorithm

- ➤ **Training dataset** is made up of observations/examples that are classified into several categories, labeled by a nominal variable.
- ► **Test dataset** contains unlabeled observations/examples
- ▶ k-NN identifies *k* records in the training data that are the "nearest" in similarity.
- ► The unlabeled test observations/examples are assigned to the class of the majority of the *k* nearest neighbors.

### Distance

Distance is calculated in the feature space

- Euclidean distance
- Manhattan distance

Euclidean distance

In a data set with n variables/features, the **Euclidean distance** between observations/examples is computed as follows

$$dist(p,q) = \sqrt{(p_1 - q_1)^2 + (p_2 - q_2)^2 + ... + (p_n - q_n)^2}$$

# Distance Example

Distance between rows.

```
## [,1] [,2]
## aa 1 1
## bb 2 2
```

## Distance Example

```
Using the distance function in R.
    dist(X)
##
              aa
## bb 1.414214
Direct calculation.
    sqrt(sum((aa-bb)^2))
## [1] 1.414214
```

# Choosing k

The balance between *overfitting* and *underfitting* the *training data* is a problem known as the **bias-variance tradeoff** 

Mean Squared Error

$$MSE(\hat{\theta}) = Var(\hat{\theta}) + Bias^{2}(\hat{\theta})$$
$$E[(\hat{\theta} - \theta)^{2}] = E[(\hat{\theta} - E[\hat{\theta}])^{2}] + E[(E[\hat{\theta}] - \theta)^{2}]$$

# Choosing k

If k is very large, nearly every training observation/example is represented in the *final vote*, the most common training class always has a majority of voters. The model would always predict the majority class. **High Bias?** 

If k is small, potentially a single nearest neighbor will determine the *final vote*, then noise may influence the prediction. **High Variance?** 

The best k values is somewhere in between.

See page 71.

# Preparing the data

► min-max normalization

$$X_{new} = \frac{X - min(X)}{max(X) - min(X)}$$

z-score normalization

$$X_{new} = \frac{X - \mu}{\sigma}$$

dummy coding for nominal variables/features



Because no abstraction occurs. There is no model, so the method is considered to be a **non-parametric** learning method.

## Example

Diagnosing *breast cancer* with k-NN algorithm.

Using R...

- loading the data
- reading the data into R
- transforming the data
- training data
- testing data
- training the model
- evaluating the model
- improving the model